intermediate frequencies, $T_{FB}(\omega)$ interpolates smoothly between these two limiting behaviours.\(^3\)

The behaviour seen in Fig. 2 is consistent with KTB dynamics, if we identify the crossover with $T_{KTB}$ of an isolated bilayer. Above $T_{KTB}$, the conductivity is predicted to scale according to\(^1\):\(^11\):

$$\sigma(\omega) = \left(\frac{k_B T}{\hbar \Omega} \right) S(\omega/\Omega)$$

(2)

The scaling function $S(\omega/\Omega)$ is constrained by the physics of the high- and low-frequency limits. As $\omega/\Omega \to \infty$, $S$ must approach $\Omega/\omega$ in order for $\sigma$ to assume its superconducting form, equation (1). At low frequencies, $S$ approaches a real constant $S_0(0)$ which characterizes the d.c. conductivity of the normal state.

By comparing the measured complex conductivity to equation (2), we can extract both the phase stiffness and correlation time at each temperature. To analyse the experimental data in terms of equation (2), we note that the phase angle of the complex conductivity, $\varphi = \tan^{-1}(\sigma_x/\sigma_y)$, equals the phase angle of $S(\omega/\Omega)$. Therefore $\varphi$ depends only on the single parameter $\Omega$, and is independent of $T_0$. With the appropriate choice of $\Omega(T)$, all the measured values of $\varphi$ should collapse to a single curve when plotted as a function of the normalized frequency $\omega/\Omega$. Knowing $\Omega(T)$, $T_0$ is obtained from a collapse of the normalized conductivity magnitude, $(k_B T/\hbar)(\Omega/\omega)^2 S(\omega/\Omega)$, to $S(\omega/\Omega)$. Figure 3 shows the collapse of the data to the phase angle and magnitude of $S$. As anticipated, $S$ approaches a real constant in the limit $\omega/\Omega \to \infty$, and approaches $\Omega/\omega$ as $\omega/\Omega \to \infty$.

When analysed further, the data reveal a confirmation of thermal generation of vortices in the normal state. In the KTB picture we expect that the d.c. conductivity will equal $k_B T/\hbar \Omega$, which is the flux-`flow' conductivity of $n_i$ free vortices with quantized flux $\Phi_m$ and diffusivity $D$ (ref. 16). Together with equation (2), this implies that $\Omega$ is a linear function of $n_i$ that is, $\Omega = \Omega n_i \Phi_m/\hbar$, where $\Phi_m$ is the area of a vortex core, $\Theta = T/T^*$ is the reduced temperature, and $\Omega = \pi S_0(0) D n_i$. Moreover, we expect that $n_i$ will be a thermally activated function, except for $T$ very close to $T_{KTB}$. The activation energy is simply $k_B /\Phi_m$, where $C$ is a non-universal constant of order unity. It follows that the fluctuation frequency depends exponentially on the reciprocal of the reduced temperature, $\Omega = (D \Phi_m/\hbar \exp(-2C/\Theta))$.

The inset to Fig. 3 is a plot of $\log(\Omega)$ versus $1/\Theta$ which shows that the exponential relation is observed over nearly four orders of magnitude. This is direct evidence that vanishing of phase coherence in our samples reflects the dynamics of thermally generated vortices. From the slope and intercept of a straight-line fit we obtain $C = 2.23$ and $\Omega_0 = 1.14 \times 10^4$ s\(^{-1}\).

In Fig. 4 we present the behaviour of the bare stiffness and phase-correlation time obtained from our measurement and modelling of $\sigma(\omega)$. The main panel contrasts $T_{FB}$ with the dynamical stiffness $T_{FB}(\omega)$ measured at 150 and 400 GHz. The inset shows $\tau$ as a function of temperature together with hatching that highlights the region where $\tau < k_B T$. The parameters displayed in Fig. 4 suggest that while phase correlations indeed persist above $T_c$, they vanish well below $T^*$.

Silica containing ordered mesopores (of nanometre-scale width) can be prepared by templating of surfactants\(^1\),\(^4\) and block copolymer\(^1\) liquid-crystalline mesophases, and interfacial phenomena have been used to control the macroscopic form of these materials, providing mesoporous particles\(^1\),\(^4\), fibres\(^5\) and films\(^6\). A variety of spherical or nearly spherical particles has been used for Physics for the opportunity to discuss this work with participants of its high-T\(_c\) workshop.

Correspondence and requests for materials should be addressed to J.O. (e-mail: jo@foxcil.bl.gov).

---

**Letters to Nature**

**Aerosol-assisted self-assembly of mesostructured spherical nanoparticles**

Yunfeng Lu*, Hongyou Fan*, Aaron Stump*, Timothy L. Ward†, Thomas Rieker* & C. Jeffrey Brinker*

*University of New Mexico/NSF Center for Micro-Engineered Materials, The Advanced Materials Laboratory, 1001 University Boulevard SE, Albuquerque, New Mexico 87106, USA

†Sandia National Laboratories, Direct Fabrication Department, 1831, Albuquerque, New Mexico 87185, USA

**Abstract**

Particles possessing nanometre-scale pores of well-defined size and connectivity are of interest for catalysis, chromatography and controlled release of drugs, as well as fillers with low dielectric constant, pigments and hosts for optically active compounds.\(^2\),\(^4\) Silica containing ordered mesopores (of nanometre-scale width) can be prepared by templating of surfactants and block copolymer liquid-crystalline mesophases, and interfacial phenomena have been used to control the macroscopic form of these materials, providing mesoporous particles, fibres and films. A variety of spherical or nearly spherical particles has been reported,\(^1\),\(^6\),\(^7\)–\(^11\), but the degree of ordering and the range of the porous mesostructures have been limited. Here we report a rapid, aerosol-based process for synthesizing solid, well-ordered spherical particles with stable pore mesostructures of hexagonal and cubic topology, as well as layered (vesicular) structures. Our method relies on evaporation-induced interfacial self-assembly confined to spherical aerosol droplets. This simple, generalizable process can be modified for the formation of ordered mesostructured thin films.
Schacht et al. first demonstrated that mesoscopically ordered hollow spheres could be prepared by interfacial reactions conducted in oil/water emulsions with varying extents of imposed shear. Huo et al. extended this general emulsion-based approach to prepare spheres with diameters of 0.1–2.0 mm. Taney and Pinnavaia condensed silica in the interlayer regions of multimamellar vesicles to form roughly spherical particles with stable lamellar mesostructures. Bruinsma et al. used spray drying to prepare hollow spherical particles or collapsed, irregular particles. These various pathways to the preparation of nominally spherical mesostructured particles have so far resulted in irregular shapes and/or particles with non-uniform or ill-defined mesostructures.

Our process starts with a homogeneous solution of soluble silica plus surfactant prepared in an ethanol/water solvent with initial surfactant concentration \( c_m \) much less than the critical micelle concentration \( c_m \). Using the apparatus depicted in Fig. 1, we generate an aerosol dispersion within a tubular reactor. In a continuous, ~6-second process, the aerosol particles are dried, heated and collected. As recently demonstrated for thin-film formation, preferential alcohol evaporation during drying enriches the particles in surfactant, water and silica, inducing micelle formation and successive co-assembly of silica–surfactant micellar species into liquid-crystalline mesophases. The resulting particles are commonly solid, with highly ordered hexagonal, cubic or vesicular mesostructures (Fig. 2). Through introduction of metal complexes or organic dyes/precursors into the starting solution, we can use the same process to prepare ordered nanocomposite particles (Fig. 3).

Figure 2 shows representative transmission electron microscope (TEM) images of calcined silica particles prepared using CTAB, Brij-58, Brij-56 or P123 templates (see Methods for details of templates). Figure 3 shows TEM images of various metal–organic– and polymer–silica nanocomposite particles. CTAB produces particles exhibiting a highly ordered hexagonal mesophase over the concentration range \( c_m = 0.06–0.16 \, \text{M} \) (Figs 2a and 5a). Many of the particles adopted a polyhedral shape that is hexagonal in cross-section, a macroscopic manifestation of the local packing geometry. Use of the non-ionic surfactants (Brij-56/58) commonly resulted in vesicular mesostructures, but cubic and hexagonal mesostructures were also attainable (Figs 2b and 3b). Distinct from related bulk and thin-film lamellar structures that collapse on calcination, the three-dimensional connectivity of the nested spherical shells comprising the vesicular mesophase mechanically stabilizes the structure against collapse during surfactant removal. Under processing conditions where the outer silica shells solidify before the drying shrinkage is complete, uniform dimpling of the shell surface results (Fig. 3c), in order to preserve the solidified shell surface area. This may be contrasted with the shrinkage-induced formation of toroidal or raisin-like collapsed morphologies commonly observed for spray-dried powders.

Figure 4 shows small-angle X-ray scattering (SAXS) data for calcined mesostructured silica particles prepared with CTAB, Brij-56 and P123 surfactants, along with the corresponding \( N_2 \) sorption isotherms (‘as-prepared’ particles had no internal surface area accessible to \( N_2 \) owing to retention of the surfactant templates). The main peak is indexed as the [100]-reflection of the hexagonal (CTAB) and vesicular mesophases. SAXS and \( N_2 \) sorption show the expected increase in \( d \)-spacing and pore size with increasing surfactant volume/molecular mass (CTAB < Brij-56 < P123).

The robustness of our evaporation-induced interfacial self-assembly (EISA) process, combined with the short residence time of the particles in the furnace, enable us to prepare a variety of mesostructured organic/silica, metal/silica and even enzyme/silica composite particles while retaining the respective structure, function and bio-activity of the guest species (A.S. and R. Bhatia, unpublished results). Furthermore, through addition of organic monomers and thermal initiators to the parent solution, we can co-organize and polymerize mesostructured silica–polymer nanocomposite particles, as recently demonstrated for coatings. The mesostructures shown in Fig. 3 illustrate the diversity of nanocomposite materials that can be prepared using this process.
constructions and materials combinations attainable by our method.

Evaporation during aerosol processing creates within each droplet a radial gradient in surfactant concentration that steepens with time and maintains a maximum concentration at the droplet surface. Starting with an initially homogeneous solution (with \( c_0 \) less than the c.m.c.), the surfactant critical micelle concentration is exceeded first at the surface of the droplet, and, as evaporation proceeds, is progressively exceeded throughout the droplet. This surfactant enrichment induces silica–surfactant self-assembly into micelles and further organization into liquid-crystalline mesophases. The radial concentration gradient and the presence of the liquid–vapour interface (which serves as a nucleating surface) causes ordered silica–surfactant liquid-crystalline domains to grow radially inward (Fig. 2d) rather than outwards from a seed. Crucial for the formation of solid, completely ordered particles is maintenance of a liquid, or liquid-crystalline, state throughout the course of the EISA process. Premature solidification would result in the formation of hollow particles and inhibit orderly self-assembly that must proceed with continual restructuring of the evolving silica–surfactant mesophase in order to accommodate drying shrinkage. Evidence for such a semi-solid state is the formation of continuous, uniform films on the collection surface when the furnace is maintained at low temperature (\( <150^\circ \text{C} \)). As shown in Fig. 5, film formation occurs via droplet coalescence. The resulting films are highly ordered, which is important for applications such as membranes, and can span hundreds of times greater in diameter than the film thickness.

We note that the curvature of the particle surface profoundly influences mesostructure development. This is evident in the comparison of CTAB-templateed particles (Fig. 2a) with the corresponding mesostructured films formed on flat substrates by EISA during dip-coating. Unlike films—which have flat liquid–vapour interfaces and show a progressive change in mesostructure (disordered → hexagonal → cubic → lamellar) with increasing surfactant concentration—particles prepared with comparable CTAB

![Figure 3 TEM micrographs of a variety of nanocomposite particles.](image)

![Figure 4 Small-angle X-ray scattering (SAXS) curves for silica particles with hexagonal (trace A) or vesicular (B and C) mesophases.](image)

**Figure 3** TEM micrographs of a variety of nanocomposite particles. a, Silica/gold nanocomposite particle with an ordered hexagonal mesostructure. Colloidal gold (particle size 1–3 nm) was prepared in inverse micelles according to the method of Brust et al., using 1-dodecanethiol as a stabilizing agent. The gold colloids were added to a silica/5 wt% CTAB sol, prepared with molar ratio TEOS:EtOH:water:HCl:CTAB = 1:0.67:0.004:0.1%. During aerosol processing, hydrophobic gold colloids partition into the hydrophobic micellar interiors and are subsequently incorporated in the hexagonal mesophase. TEM and X-ray diffraction indicate \( d_{100} = 60 \) Å (compared to 32.5 Å; Fig. 2a), consistent with incorporation of the gold colloids in the hexagonal silica mesophase. b, Fluorescent silica/rhodamine B nanocomposite particles exhibiting a hexagonal mesophase. The sol was prepared by adding 0.8 wt% rhodamine B to a silica/4.2 wt% Brij-56 sol prepared with molar ratio TEOS:EtOH:water:HCl:Brij-56 = 1:13:67:0.004:0.068. Inset, optical photomicrograph of the fluorescence emission imaged through a rhodamine B filter, confirming retention of the dye structure. Samples were exhaustively washed before optical microscopy. c, Silica/polymer nanocomposite particle showing puckered vesicular mesostructure (inset, SEM image showing uniform periodic dimpling). The sol was prepared by adding poly(propylene glycol dimethylacrylate) (PPO, molecular mass 660) and thermal initiator, 1,1'-azobis(1-cyclohexanecarbonitrile) (ACN) to a silica/5 wt% P123 sol prepared with molar ratio TEOS:ethanol:water:HCl:P123:PPO:ACN = 1:22:5:0.004:0.0096:0.025:0.009. During aerosol processing, the oligomer and initiator are incorporated into the hydrophobic portion of the template bilayers resulting in thermally initiated polymerization of PPO. d, Silica/polymer nanocomposite particle showing reticulated foam structure. The sol was prepared as in c but with molar ratio TEOS:ethanol:water:HCl:P123:PPO:ACN = 1:13:67:0.004:0.0096:0.025:0.009. The greater water concentration compared to c resulted in micelle formation (in the starting sol) and incorporation of PPO and ACN into the micellar interiors. Subsequent micelle coalescence combined with thermally initiated polymerization during aerosol processing resulted in the reticulated nanostructure.

**Figure 4** Small-angle X-ray scattering (SAXS) curves for silica particles with hexagonal (trace A) or vesicular (B and C) mesophases. Samples A and C were prepared as in Fig. 2a and c, respectively. Sample B was obtained for calcined particles showing a vesicular mesostructure (\( d_{100} = 66 \) Å). The sol was prepared using 4.2 wt% Brij-56 as the surfactant template, and molar ratio TEOS:EtOH:water:HCl:Brij-56 = 1:13:67:0.004:0.068. Inset, Corresponding \( N_2 \) adsorption--desorption isotherms, BET surface areas, and pore diameters. (We note that the calculated pore diameter of sample A is slightly less than 2.0 nm, the lower limit of mesoporosity according to the IUPAC definition. Thus the validity of the BET expression is questionable). SALS experiments were performed at the University of New Mexico/Sandia National Laboratories SAXS facility. Samples (~0.5 mm thick) were prepared by sprinkling powder on adhesive cellophane tape used as a 1.5-cm-diameter window. SAXS data were collected (30 min per run) using the 5-m pinhole instrument in short geometry (0.3 < \( q < 7 \) \( \text{nm}^{-1} \), where \( q \) is defined as \( 4\pi/\lambda \sin(\theta/2) \), and \( \theta \) is the scattering angle). SAXS data are uncorrected for background. Hydraulic pore diameters were calculated from the pore volume and BET surface area.
coalescence on a holey carbon grid. For holes much greater in diameter than the film thickness, formation is possible by avoidance of particle solidification. The semi-solid nature mesostructure before complete coalescence. From a film deposition route. A 5 wt% P123 sol (identical to that in Fig. 2c) was used.

Methods

Conclusion that, because the liquid–vapour interface serves as a nucleating surface for liquid-crystal growth, the high curvature concentration show only disordered or hexagonal mesophases. We conclude that, because the liquid–vapour interface serves as a nucleating surface for liquid-crystal growth, the high curvature imposed by this interface alters the generally observed relationship between the surfactant packing parameter and the resulting mesostructure. Although CTAB commonly forms lamellar mesophases in bulk and thin-film samples, it appears that this molecule cannot pack into a cone truncated by surfaces of high opposite curvature, as needed to direct the vesicular mesostructure. Only surfactants containing ethylene oxide (EO) blocks consistently gave vesicular mesophases.

Precursor solutions were synthesized by the addition of cationic surfactant

Figure 5 TEM images of mesostructured films formed by an aerosol-assisted thin film deposition route. A 5 wt% P123 sol (identical to that in Fig. 2c) was used. a, Cross-sectional TEM image of hexagonal mesostructured film deposited on silicon substrate. b, Plan-view image of hexagonal mesostructured film deposited on holey carbon grid. c, TEM image of corresponding aerosol droplets during formation of mesostructured films by an aerosol-assisted thin film deposition route. a, Cross-sectional TEM image of hexagonal mesostructured film deposited on silicon substrate. b, Plan-view image of hexagonal mesostructured film deposited on holey carbon grid. c, TEM image of corresponding aerosol droplets during deposition of mesostructured films by an aerosol-assisted thin film deposition route.